
Please note that the assigned homework may not be enough for some people. If the concepts are still a little fuzzy after doing the homework, please take advantage of the other problems in Mano and/or see me for more problems. Also note that there are a few zero point questions. These are optional. You can use them if you need additional practice.

When you can verify an answer, do so.

Show your work.

Mano and Kime have some nice problems in Chapter 6. I'll be using a few of them. Problem eight will take a while.

1. *(0 pts.)* Mano 6.5.

2. Design a fancy turn signal controller for an automobile. The driver can generate three binary signals:
   - L: turn left
   - R: turn right
   - E: emergency lighting

   Zero or one of these signals may be active at a time.

   (a) *(10 pts.)* (encoder review) Design an encoder to get the necessary information from the driver to the back of the car. Equations are sufficient; you need not draw circuit diagrams. Use these codes:

<table>
<thead>
<tr>
<th>Signals (LRE)</th>
<th>Encoded signal (AB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>000</td>
<td>00</td>
</tr>
<tr>
<td>100</td>
<td>10</td>
</tr>
<tr>
<td>010</td>
<td>01</td>
</tr>
<tr>
<td>001</td>
<td>11</td>
</tr>
</tbody>
</table>

   (b) *(10 pts.)* (decoder review) Design the corresponding decoder from standard 1-input decoders and AND gates. Show a schematic for the decoder on which all inputs and outputs are carefully labeled.

   (c) The decoder was for use in debugging. From now on, you’ll be using the encoded signal. Your turn indicator is a horizontal linear array of three (amazingly bright) LEDs controlled by the I, J, and K signals. If the left turn signal is on, you should cycle repeatedly though the following values for I, J, and K:

   001, 010, 100.

   If the right turn signal is on, cycle through these values:

   100, 010, 001.

   If the emergency lighting signal is on, cycle through these values:

   000, 010.

   1
If no signal is on, the LEDs should all be off.
When the input signal (no action, left turn, right turn, emergency lighting) changes, it is fine for
there to be a slight delay before the new pattern is initiated. For example, if the current output
is 100 and the left turn signal is on, a change to emergency lighting may go through 001 before
starting the normal emergency lighting cycle.

i. (10 pts.) Draw the state diagram for a synchronous Moore FSM implementing these re-
quirements.

ii. (5 pts.) Show the state table for the FSM.

iii. (5 pts.) Assign states, and redo the state table.

iv. (10 pts.) Assuming access to D flip-flops, use Karnaugh maps to derive the state variable
equations and output variable equations. There are multiple ways to implement this machine.
Some have simpler output variable functions at the cost of more state variables. Others reduce
the number of state variables but require more complicated output variable functions.

3. (0 pts.) Design of a special ALU
Mr. Sinha needs a special arithmetic unit for his work. He has to perform one of several operations
on two 3-bit 2's complement numbers and he needs a circuit which can do this for him depending on
his choice of actions. For the 2 numbers A and B (3 bit each), he would like to perform the following
operations:
(a) A + B
(b) A - B
(c) 2A
(d) A + 2B

Design a circuit using MUXs, AND gates, inverters and only one 4-bit ripple-carry adder assuming
that the four choice above are used as Control Inputs (2 bits) with encodings 00, 01, 10, and 11 in that
order respectively. You may ignore overflow. The output should be a 4-bit number.

4. (10 pts.) Sequence recognizer
Design a sequential circuit using D flip-flops and logic gates that can recognize the sequence “00110”.
If this sequence has just occurred, the output, \( Q \), should be set to 1. Otherwise, \( Q \) should be 0.

5. Consider the state diagram in Figure 1.

(a) (1 pts.) Is this a Moore or Mealy machine?
(b) (4 pts.) Write the state table for this machine.
(c) (5 pts.) Do state assignment and rewrite the state table.
(d) (10 pts.) Use Karnaugh maps or Quine-McCluskey’s algorithm to derive minimal SOP equations
for the state variables and output.

6. Consider the following state table

<table>
<thead>
<tr>
<th>Current state</th>
<th>Next state/Q when i=0</th>
<th>Next state/Q when i=1</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>A/0</td>
<td>C/X</td>
</tr>
<tr>
<td>B</td>
<td>D/0</td>
<td>D/0</td>
</tr>
<tr>
<td>C</td>
<td>A/1</td>
<td>B/1</td>
</tr>
<tr>
<td>D</td>
<td>D/0</td>
<td>C/0</td>
</tr>
</tbody>
</table>
Figure 1: A finite state machine

(a) (5 pts.) Is this a Moore or Mealy machine? Justify your answer in up to three sentences.

(b) (5 pts.) Do state assignment, then derive minimal SOP state and output equations.

7. (0 pts.) Draw the state diagram and state table for a single-output Moore machine. The machine must outputs a 1 if and only if the two most recent inputs were both 1s. If the two most recent inputs were not both 1s, the machine should output a 0. If the machine ever receives a sequence of two or more 0s, it must never again output anything but a 0.