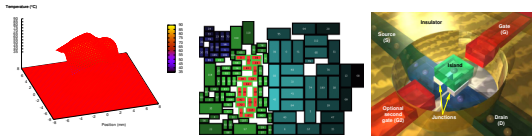


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- Cooling fundamentals
- Multiple cooling methods
 - Combinations often used in real applications

Conduction

$$P = A\kappa \cdot \Delta T/d$$

- P : Power in W
- A : Area
- κ : Thermal conductivity
- ΔT : Difference in temperature
- d : Depth

Radiative interaction

$$k = \frac{A \cos \theta}{4\pi r^2}$$

- k : Patch interaction coefficient
- A : Patch area
- θ : Angle between patches
- r : Distance between patches

Convection

Convection:

$$P = 2hA(T_S - T_F)$$

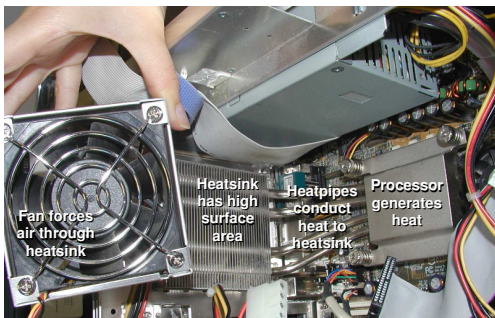
$$h \approx k_1(T_S - T_F)^{1/4}$$

Therefore,

$$I \propto (T_S - T_F)^{5/4}$$

- P : Power in W
- h : Heat transfer coefficient
- k_1 : Constant for film coefficient and film conductance (0.0021 W/(m² K))
- A : Area of one side of plate
- T_S and T_F : Solid and fluid temperatures

Multiple modes common in real applications



Radiative cooling

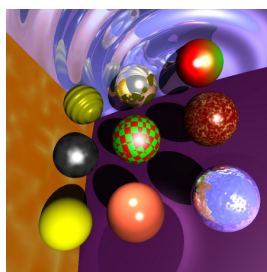
$$P = Ae\sigma T^4 - Ae\sigma T_A^4$$

- P : Power in W
- A : Surface area
- e : Emissivity of surface [0:1]
 - 0.3 for Cu, 0 for rough black surface
- σ : Stefan-Boltzmann constant = 5.67×10⁻⁸ W/(m² K)
- T : Temperature
- T_A : Ambient temperature
- Why does a thermos have mirrored walls?

Other uses of radiation



Radiosity



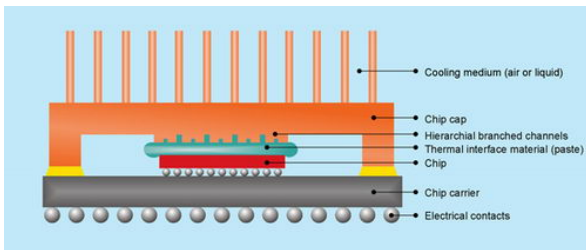
Ray tracing

Forced air heatsink

How to improve?

- Increase fluid flow rate, decreasing surface film thickness
- Or increase film conductance
 - Increases k_f
- Increase surface area
- Increase temperature difference (?)
- Increase conductance to heatsink

Heatsink attachment



- IBM proposes cutting tree-structure trenches in chip cap
- Thinner interface material, less pressure, few details

Ion pump cooling

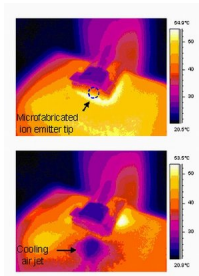
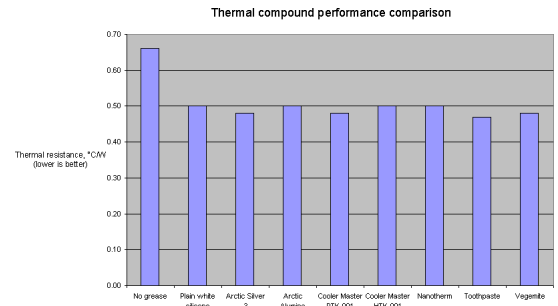


Image credit to N. Jewell-Larsen.

Liquid cooling

- Specific heat capacity of water $4 \times$ air
- Thermal conductivity $25 \times$ air
- Passive: Vat of oil
- Active: Recirculating pump
 - Where does heat go?
- Microchannel

Thermal compounds



Credit to Dan's Data and Vegemite.

Heatsink attachment

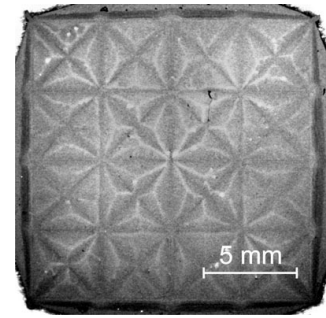


Image credit to IBM.

Ion pump operation

- High-voltage positive electrode ionizes air
- Ions travel to negative electrode (chip)
- Air pulled along
- Cooled a few mm^2 by 25°C this way
- Claiming $180 \text{ W}/(\text{mm}^2 \text{ K})$ at 4.5 kV, 2 mm^2

Microchannel

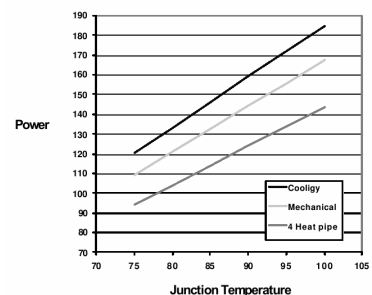


Image credit to Cooligy.

Phase change

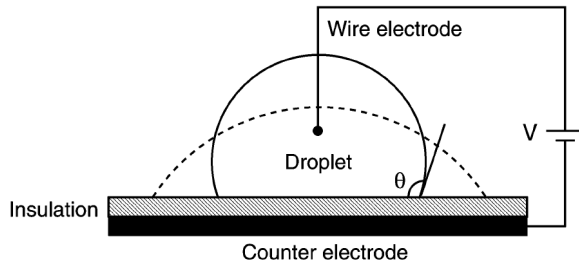
- Abrupt change in heat capacity
- Result in transfer in large amount of energy
 - Rate bound results in mixed state
- Latent heat: Amount of energy released or absorbed during evaporation
- 855 J/g for ethyl alcohol at 78°C
- 1086 J/g for methyl alcohol at 65°C
- 2258 J/g for water at 100°C

20

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Temperature-Aware and Low-Power Design and Synthesis

Electrowetting



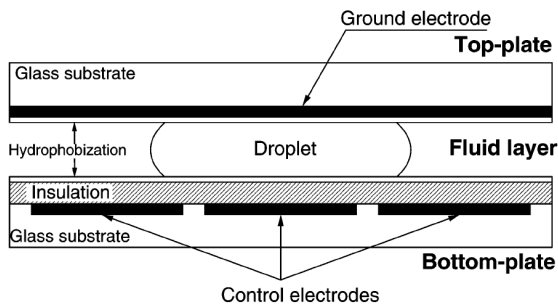
Credit to M. G. Pollack for image.

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Electrowetting microactuator



Credit to M. G. Pollack for image.

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Thermoelectric interdependence

In the same electric field, hot electrons travel faster than cold electrons inducing heat flow

$$\vec{J}_Q = D\vec{E}$$

Charge flows faster from hot regions to cold regions

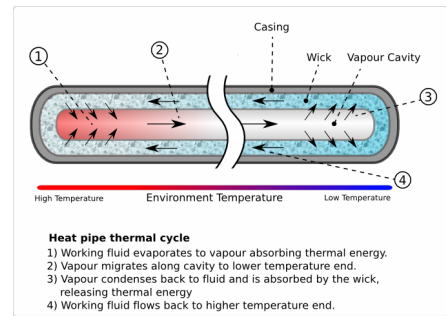
$$\vec{J}_e = C\vec{G}$$

27

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Heat pipe



Heat pipe thermal cycle

- 1) Working fluid evaporates to vapour absorbing thermal energy.
- 2) Vapour migrates along cavity to lower temperature end.
- 3) Vapour condenses back to fluid and is absorbed by the wick, releasing thermal energy.
- 4) Working fluid flows back to higher temperature end.

21

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Electrowetting

$$\gamma_{SL} = \gamma_{SL}^0 - \frac{\epsilon V^2}{2 \cdot d}$$

- γ_{SL} : Solid-liquid interfacial tension
- V applied voltage
- γ_{SL}^0 : Solid-liquid interfacial tension at $V = 0$
- ϵ : Dielectric constant for insulating film
- d : thickness of insulating film

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Electrical and thermal fields

$$\vec{J}_Q = + \kappa \vec{G}$$

$$\vec{J}_e = \delta \vec{E}$$

- \vec{J}_Q : Heat flow
- κ : Thermal conductivity
- \vec{G} : Temperature gradient
- \vec{J}_e : Electrical current
- δ : Electrical conductivity
- \vec{E} : Electric potential gradient

Credit to Prof. Grayson for his notes on this topic.

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Thermoelectric effects

$$\vec{J}_e = \delta \vec{E} + C\vec{G}$$

$$\vec{J}_Q = \kappa \vec{G} + D\vec{E}$$

$$D = CT$$

where T is temperature.

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Thermoelectric devices

Solve for \vec{E} and \vec{J}_Q

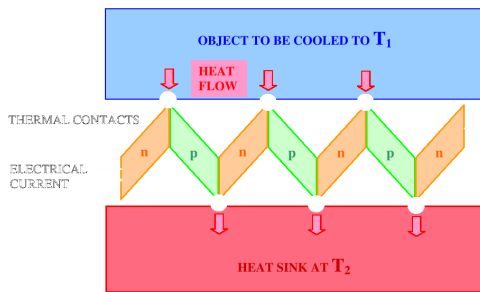
$$\begin{aligned}\vec{E} &= \vec{J}_e / \delta - S \vec{G} \\ \vec{J}_Q &= \pi \vec{J}_e + (\kappa - \delta S \pi) \vec{G} \\ \pi &= ST\end{aligned}$$

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Peltier heat pumps



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Stacked Peltier



Credit for image to TE Technology, Inc.

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Peltier effect

$$\vec{J}_Q = \pi \vec{J}_e \Rightarrow I_Q = \pi I_e$$

where I_q is the total heat current and I_e is the total electrical current. Within a piece of metal

$$I_Q^{in} = I_Q^{out} = \pi I_e$$

However, at junction

$$I_Q^{in} - I_Q^{out} = (\pi_A - \pi_B) I_e$$

Thus heat can be transported from one junction to another via charge carriers.

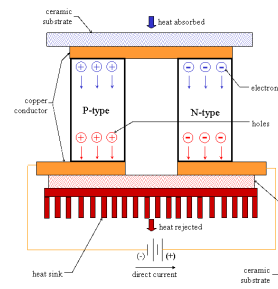
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Peltier heat pumps

Schematic of a Thermoelectric Cooler



Credit for image to TE Technology, Inc.

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