1 Reference material

	C_{OX} (fF/µm^2)	C_O (fF/µm)	C_j (fF/µm^2)	m_j	ϕ_b (V)	C_{jsw} (fF/µm)	m_{jsw}	ϕ_{bsw} (V)
NMOS	6	0.31	2	0.5	0.9	0.28	0.44	0.9
PMOS	6	0.27	1.9	0.48	0.9	0.22	0.32	0.9

MODELS FOR CMOS DEVICES

CMOS (0.25 µm) – Unified Model.

	V_{T0} (V)	γ ($V^{0.5}$)	V_{DSAT} (V)	k' (A/V^2)	λ (V^{-1})
NMOS	0.43	0.4	0.63	115×10^{-6}	0.06
PMOS	–0.4	–0.4	–1	-30×10^{-6}	–0.1

CMOS (0.25 µm) – Switch Model (R_{eq})

V_{DD} (V)	1	1.5	2	2.5
NMOS (kΩ)	35	19	15	13
PMOS (kΩ)	115	55	38	31

CMOS (0.25 µm) – BSIM Model

See Website: *http://bwrc.eecs.berkeley.edu/IcBook*

Name	Value
kT/q	25.875 mJ/C
NMOSFET I_S	21.0 pA
PMOSFET I_S	41.8 pA
n (for I_D calculation)	1.5

VALUES OF MATERIAL AND PHYSICAL CONSTANTS

Name	Symbol	Value	Units
Room temperature	T	300 (= 27°C)	K
Boltzman constant	k	1.38×10^{-23}	J/K
Electron charge	q	1.6×10^{-19}	C
Thermal voltage	$\phi_T = kT/q$	26	mV (at 300 K)
Intrinsic Carrier Concentration (Silicon)	n_i	1.5×10^{10}	cm^{-3} (at 300 K)
Permittivity of Si	ε_{si}	1.05×10^{-12}	F/cm
Permittivity of SiO_2	ε_{ox}	3.5×10^{-13}	F/cm
Resistivity of Al	ρ_{Al}	2.7×10^{-8}	Ω-m
Resistivity of Cu	ρ_{Cu}	1.7×10^{-8}	Ω-m
Magnetic permeability of vacuum (similar for SiO_2)	μ_0	12.6×10^{-7}	Wb/Am
Speed of light (in vacuum)	c_0	30	cm/nsec
Speed of light (in SiO_2)	c_{ox}	15	cm/nsec

$$P = P_{SWITCH} + P_{SHORT} + P_{LEAK}$$

$$P_{SWITCH} = C \cdot {V_{DD}}^2 \cdot f \cdot A$$

$$\dagger\, P_{SHORT} = \frac{b}{12}(V_{DD} - 2 \cdot V_T)^3 \cdot f \cdot A \cdot t$$

$$P_{LEAK} = V_{DD} \cdot (I_{SUB} + I_{GATE} + I_{JUNCTION} + I_{GIDL})$$

C : total switched capacitance

f : switching frequency

b : MOS transistor gain

t : rise/fall time of inputs

V_{DD} : high voltage

A : switching activity

V_T : threshold voltage

† P_{SHORT} usually $\leq 10\%$ of P_{SWITCH}

Smaller as $V_{DD} \to V_T$

$A < 0.5$ for combinational nodes, 1 for clocked nodes.

FORMULAS AND EQUATIONS

Diode

$$I_D = I_S(e^{V_D/\phi_T} - 1) = Q_D/\tau_T$$

$$C_j = \frac{C_{j0}}{(1 - V_D/\phi_0)^m}$$

$$K_{eq} = \frac{-\phi_0^m}{(V_{high} - V_{low})(1-m)} \times [(\phi_0 - V_{high})^{1-m} - (\phi_0 - V_{low})^{1-m}]$$

MOS Transistor

$$V_T = V_{T0} + \gamma(\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{|-2\phi_F|})$$

$$I_D = \frac{k'_n}{2}\frac{W}{L}(V_{GS} - V_T)^2(1 + \lambda V_{DS}) \text{ (sat)}$$

$$I_D = \upsilon_{sat} C_{ox} W\left(V_{GS} - V_T - \frac{V_{DSAT}}{2}\right)(1 + \lambda V_{DS}) \text{ (velocity sat)}$$

$$I_D = k'_n \frac{W}{L}\left((V_{GS} - V_T)V_{DS} - \frac{V_{DS}^2}{2}\right) \text{ (triode)}$$

$$I_D = I_S e^{\frac{V_{GS}}{nkT/q}}\left(1 - e^{-\frac{V_{DS}}{kT/q}}\right) \text{ (subthreshold)}$$

Deep Submicron MOS Unified Model

$I_D = 0$ for $V_{GT} \le 0$

$I_D = k'\frac{W}{L}\left(V_{GT}V_{min} - \frac{V_{min}^2}{2}\right)(1 + \lambda V_{DS})$ for $V_{GT} \ge 0$

with $V_{min} = \min(V_{GT}, V_{DS}, V_{DSAT})$

and $V_{GT} = V_{GS} - V_T$

MOS Switch Model

$$R_{eq} = \frac{1}{2}\left(\frac{V_{DD}}{I_{DSAT}(1 + \lambda V_{DD})} + \frac{V_{DD}/2}{I_{DSAT}(1 + \lambda V_{DD}/2)}\right) \approx \frac{3}{4}\frac{V_{DD}}{I_{DSAT}}\left(1 - \frac{5}{6}\lambda V_{DD}\right)$$

Inverter

$V_{OH} = f(V_{OL})$

$V_{OL} = f(V_{OH})$

$V_M = f(V_M)$

$$t_p = 0.69 R_{eq} C_L = \frac{C_L(V_{swing}/2)}{I_{avg}}$$

$P_{dyn} = C_L V_{DD} V_{swing} f$

$P_{stat} = V_{DD} I_{DD}$

Static CMOS Inverter

$V_{OH} = V_{DD}$

$V_{OL} = GND$

$V_M \approx \frac{rV_{DD}}{1 + r}$ with $r = \frac{k_p V_{DSATp}}{k_n V_{DSATn}}$

$V_{IH} = V_M - \frac{V_M}{g}$ $\quad V_{IL} = V_M + \frac{V_{DD} - V_M}{g}$

with $g \approx \frac{1 + r}{(V_M - V_{Tn} - V_{DSATn}/2)(\lambda_n - \lambda_p)}$

$$t_p = \frac{t_{pHL} + t_{pLH}}{2} = 0.69 C_L\left(\frac{R_{eqn} + R_{eqp}}{2}\right)$$

$P_{av} = C_L V_{DD}^2 f$

Interconnect

Lumped RC: $t_p = 0.69\ RC$

Distributed RC: $t_p = 0.38\ RC$

RC-chain:

$$\tau_N = \sum_{i=1}^{N} R_i \sum_{j=i}^{N} C_j = \sum_{i=1}^{N} C_i \sum_{j=1}^{i} R_j$$

Transmission line reflection:

$$\rho = \frac{V_{refl}}{V_{inc}} = \frac{I_{refl}}{I_{inc}} = \frac{R - Z_0}{R + Z_o}$$

CMOS COMBINATIONAL LOGIC

Transistor Sizing using Logical Effort

$$F = \frac{C_L}{C_{g1}} = \prod_1^N \frac{f_i}{b_i} \qquad G = \prod_1^N g_i \qquad D = t_{p0}\sum_{j=1}^{N}\left(p_j + \frac{f_j g_j}{\gamma}\right)$$

$$B = \prod_1^N b_i \qquad H = FGB \qquad D_{min} = t_{p0}\left(\sum_{j=1}^{N} p_j + \frac{N(\sqrt[N]{H})}{\gamma}\right)$$