Introduction to Computer Engineering - EECS 203

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Introduction to number systems

This works for any base. Convert 2,0123 from base-3 to base-10.

$$\begin{aligned}2\cdot3^3+0\cdot3^2+1\cdot3^1+2\cdot3^0\\2\cdot27+0\cdot9+1\cdot3+2\cdot1\\54+0+3+2\\59_{10}\end{aligned}$$

Conversion works for any base

Review: For base-10, given an n-digit number in which d_i is the ith digit, the number is

$$\sum_{i=1}^n 10^{i-1} \cdot d_i$$

For base-b, given an n-digit number in which d_i is the ith digit, the number is

$$\sum_{i=1}^{n} \cdot b^{i-1} \cdot d_{i}$$

Binary

Introduction to number systems

Consider a base-10 number: 1 293

$$\frac{1}{1}, \frac{293}{1} = \frac{1}{1} \cdot 10^3 + \frac{1}{2} \cdot 10^2 + \frac{9}{10^3} \cdot 10^1 + \frac{3}{10^3} \cdot 10^0$$

For base-10, given an n-digit number in which d_i is the ith digit, the number is

$$\sum_{i=0}^{n} 10^{i-1} \cdot d_i$$

Introduction to number systems

Convert 59_{10} from base-10 to base-3. Repeatedly divide by the greatest power of b (the base) that is less than the number.

Remainder	Try dividing	Digit	Comment
59	$3^4 = 81$	0	Too big
$59 - 0 \cdot 81 = 59$	$3^3 = 27$	2	O.K.
$59 - 2 \cdot 27 = 5$	$3^2 = 9$	0	Too big
$5 - 0 \cdot 9 = 5$	$3^1 = 3$	1	O.K.
$5 - 1 \cdot 3 = 2$	3 ⁰	2	O.K.

 $02012_3 = 2012_3$

Useful bases

- 2: Also called binary. Most fundamental base in digital logic. Know this like the back of your hand.
- 8: Also called octal. Sometimes used by programmers. Prefer base 16.
- 10: Also called decimal or Arabic.
- 16: Also called hexadecimal or simple hex. One of the most compact and beautiful representations for digital computer programmers.

Decimal

- Most commonly used by human beings.
- Also called Arabic.
 - Actually developed in India and brought to Europe via Arabian
- Largely replaced Roman numerals, which were more cumbersome when writing the large and complicated numbers used in astronomy and wide-spread trade.

• Representation of positive numbers same in most systems • A few special-purpose alternatives exist, e.g., Gray code

Often prefixed with 0x. What is 0xFF?

Computer geek culture reference

- Spelling things in ASCII (hex or binary) • This is one of the lower forms of geek culture, akin to bad puns
- However, at least one university has things written into its buildings with subtle brick patterns in ASCII binary

4a6934207375616e34206a69312073686534206a69342068656e332068616f332077616e3221

Alternatives exist for signed numbers

Reading assignment

- M. Morris Mano and Charles R. Kime. Logic and Computer Design Fundamentals. Prentice-Hall, NJ, third edition, 2004
- Sections 5.1-5.6